

## What are the effects of linear mixing and how can they be mitigated for Triple-Exposure PTV

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Particle Tracking Velocimetry (PTV)	Linear Unmixing
Finding a flow field in a region of interest through placing small (~10um) tracer particles in a fluid and imaging it. Computational methods can track particles through their motion	A technique to remove artefacts in from the Bayer matrix. Some work has been done on this for PTV and closely related fields, but it is primarily developed through microscopy and remote sensing.
Bayer matrix	Gigatrack
A pattern of colour filters over monochrome sensors to allow camera sensors to reconstruct colour data	MATLAB scripts to allow for low-cost PTV, developed by John Lawson

### The problem:

PTV hardware is typically very expensive, so why not just use cheaper hardware?

This also allows for more temporal information on each image through multiple colour channels recording at different times

**Consumer hardware leads to bad-quality data – can processing make it acceptable quality?**

Imperfect colour filters lead to a large number of particles with zero velocity

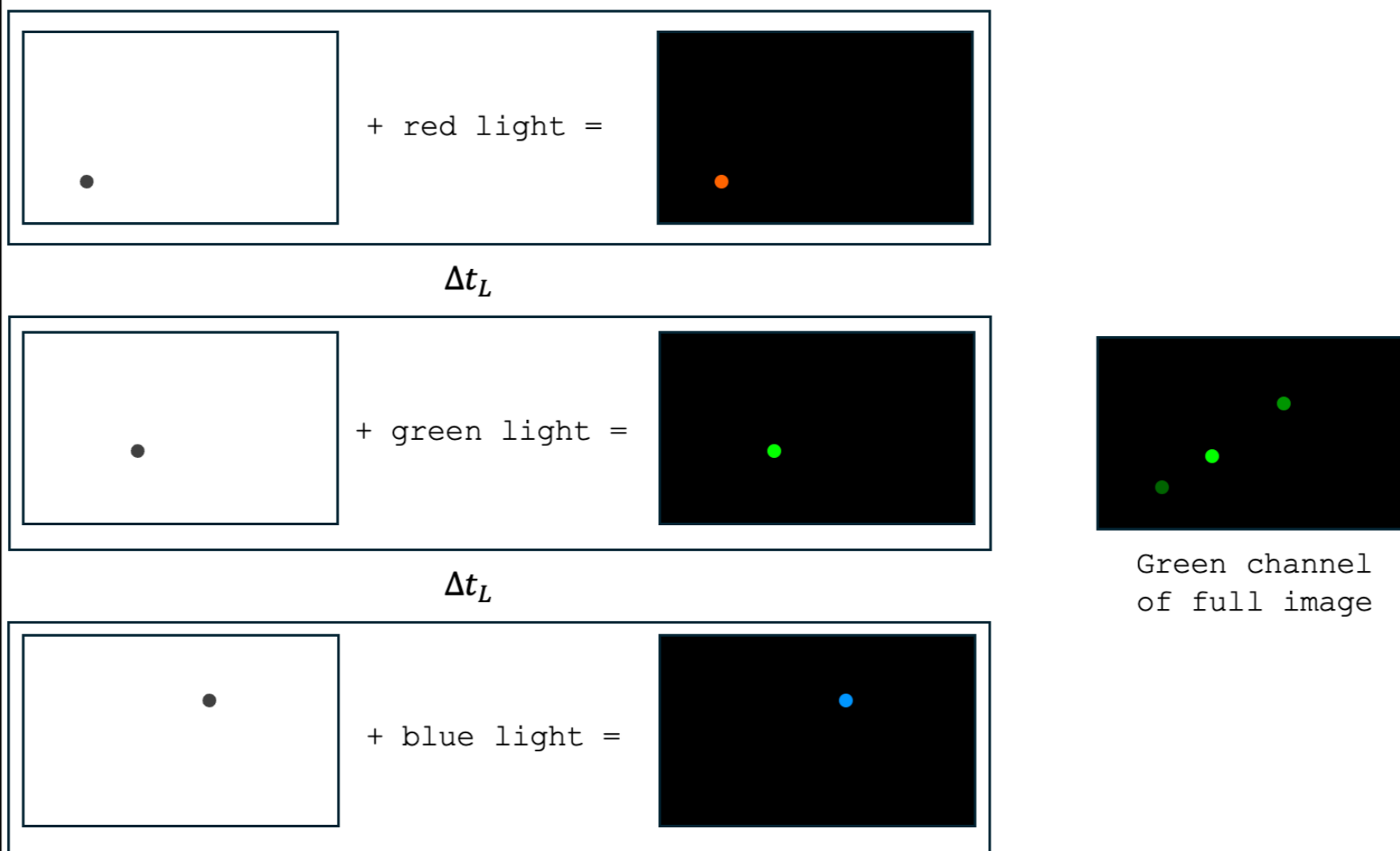
### The solution:

Get an undergrad to look at it

Minimise number of false particles while maximising number of real particles, so existing techniques can be used

Previous solutions include:

- Find the correlation coefficient of the channels of light, if it is sufficiently low, reject
- Find how much each light affects each type of sensor on the camera
- Use cameras that reject these errors



### More information on how it works:

Wang [1] shows the full method used  
Charonko [2] mentions it in passing

Representative sample data gives the correlation between one channel and another  
These 9 values are put in a matrix.  
Test data is then captured, with each pixel being a vector of colour data  
The colour data is multiplied by the inverse of the matrix to clean the test data.

### Other applications of the technique

Flourescent markers in microscopy [3] (more relevant)  
Determining ground composition in remote sensing [4] (less relevant)

$$\begin{bmatrix} S_r \\ S_g \\ S_b \end{bmatrix} = \begin{pmatrix} a \begin{bmatrix} C_{RR} & C_{RG} & C_{RB} \\ C_{GR} & C_{GG} & C_{GB} \\ C_{BR} & C_{BG} & C_{BB} \end{bmatrix} \end{pmatrix} \begin{bmatrix} A_r \\ A_g \\ A_b \end{bmatrix}$$

### Computational section

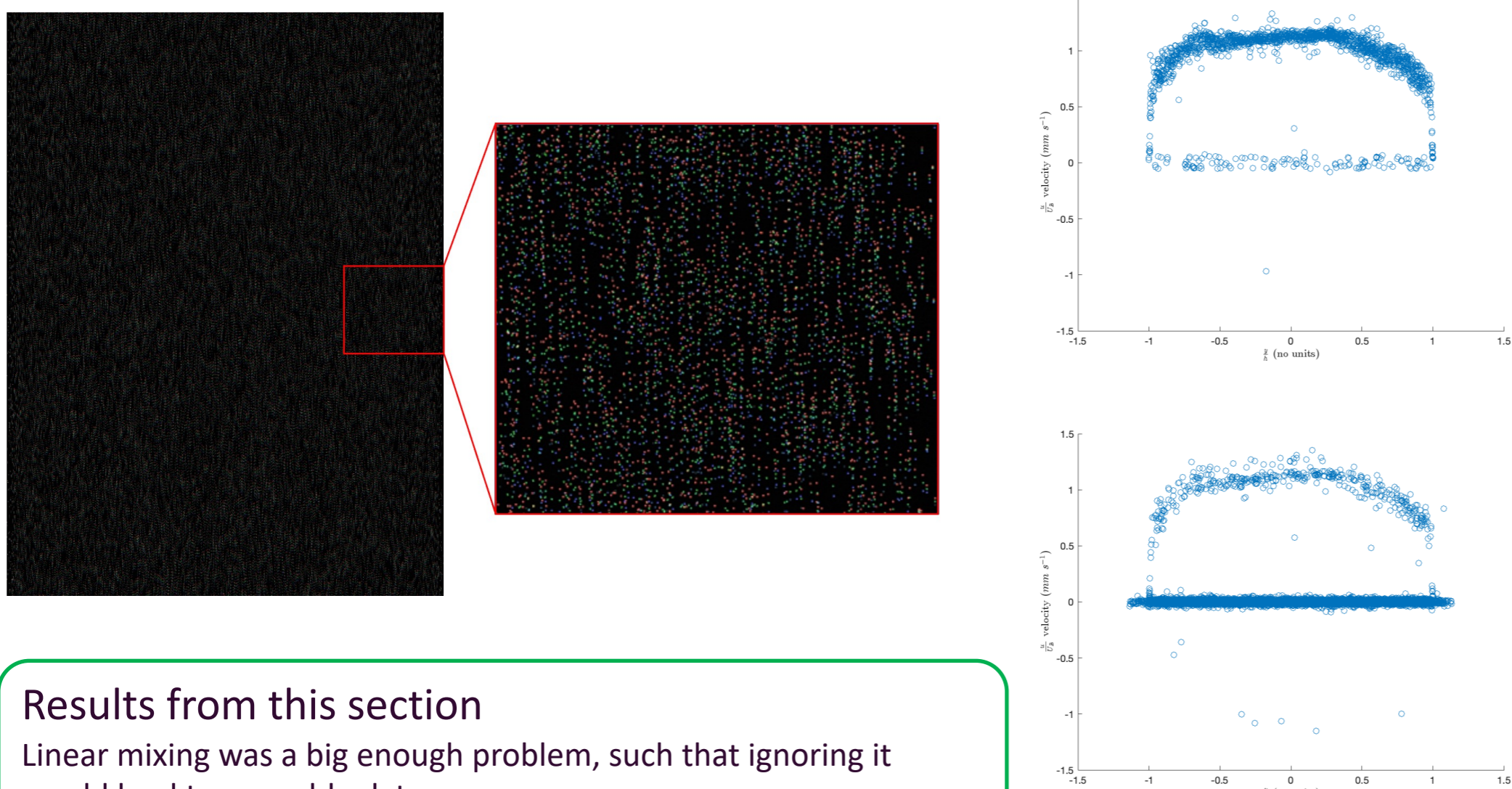
This section focused on extending Gigatrack to allow for simulation of the linear mixing. With this developed, methods for linear unmixing could be tested to validate them.

There was already a matrix to show how the camera will respond to light, which was modified to represent linear mixing.

Linear unmixing was implemented through a preprocessing step, which saves the files in a distinct directory.

This allows for easy comparison between data with and without treatment.

Many different plots of the flow were made, and using this information, conclusions about the efficacy of the correction algorithm could be made

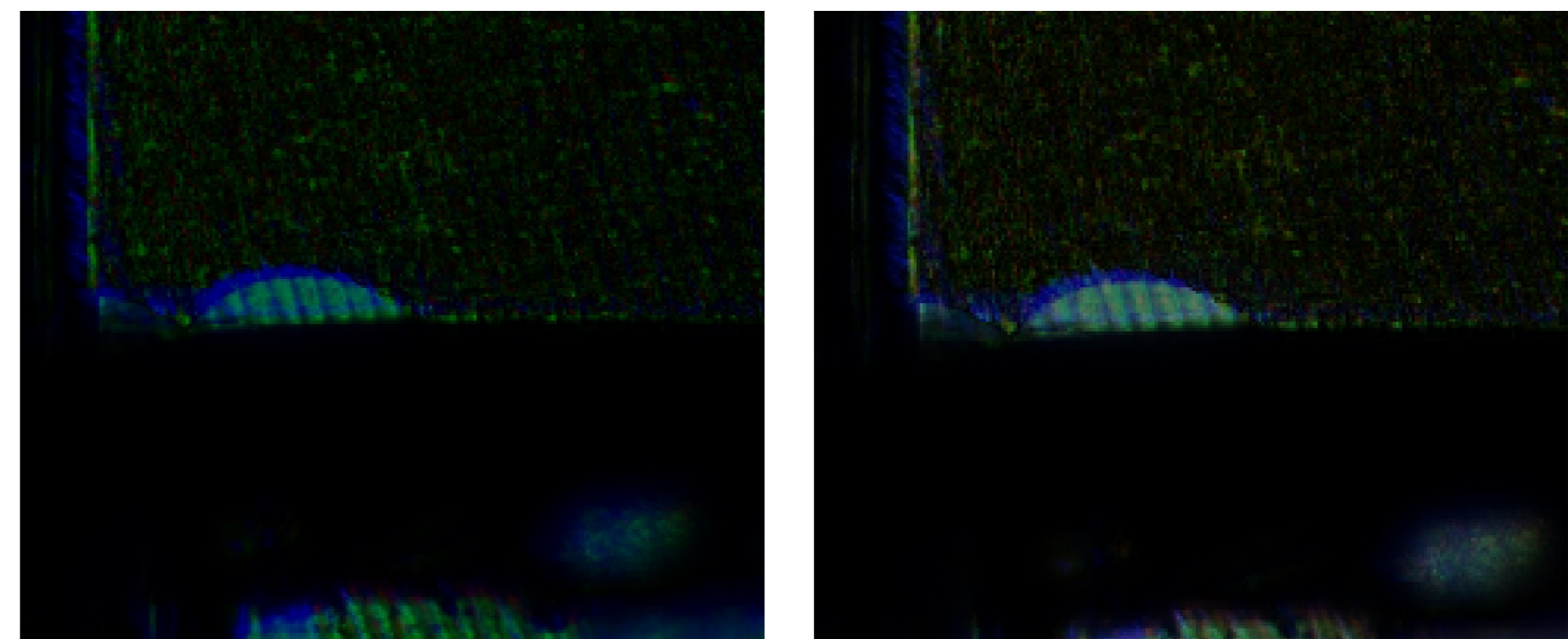
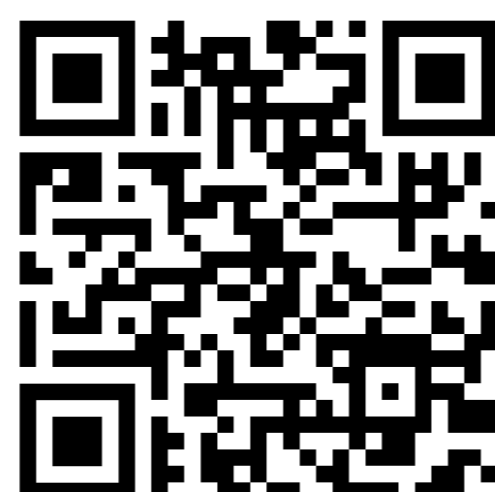
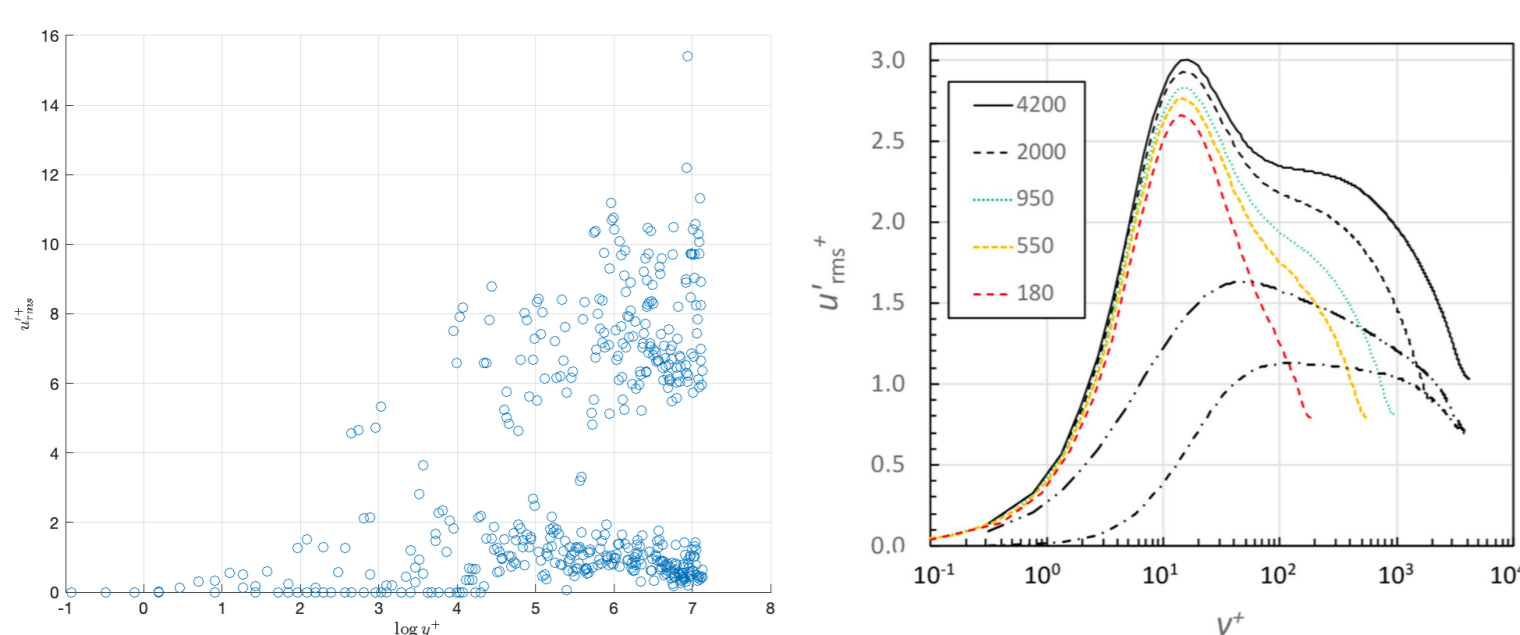


### Results from this section

Linear mixing was a big enough problem, such that ignoring it would lead to unusable data.

While imperfect, the method presented was adequate to get a good degree of accuracy from imperfect image.

The corrections were not able to fully remove all erroneous data, but it was incredibly effective in correcting most of it.



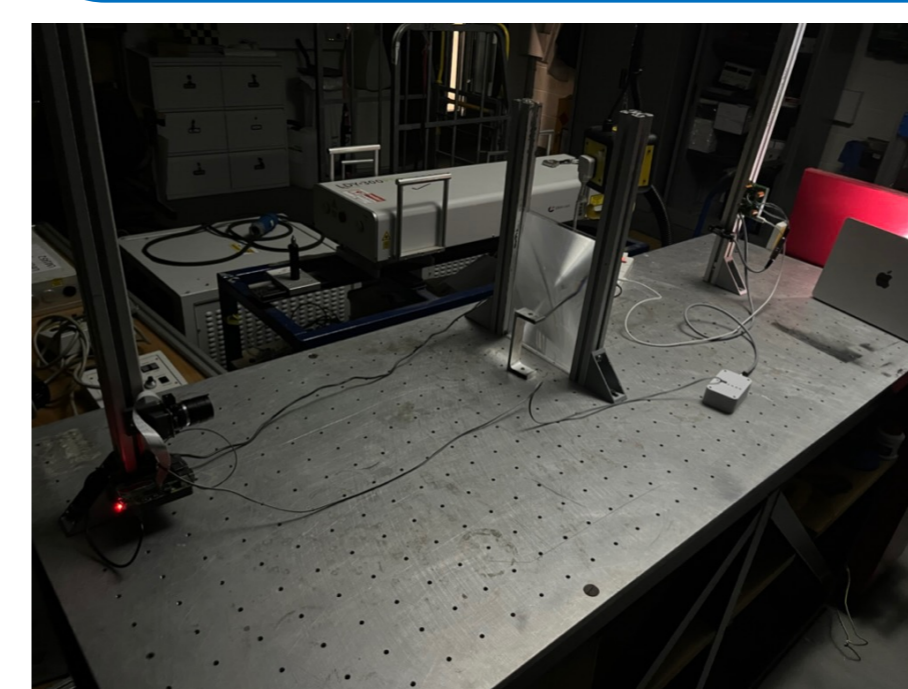
### Experimental section

Key aims were to validate that the techniques developed could be extended to real data  
Low-cost solutions added the issue of an inhomogenous background, which was overcome  
The methods used were not as simple as in the computational section due to practical issues with measurement volume and time pressures.

Tooling was developed to allow images to be used in MATLAB  
Shadows of particles were captured, so they needed to be inverted to be as Gigatrack expects.

### Results

There are additional real-world effects that need to be accounted for (chromatic aberration primarily)  
Software is easier than hardware  
The system works



### Future work

- Improve speed of processing to allow for processing of large datasets
- Further iteration on background removal
- Investigate ways to improve accuracy of synthetic data
- More experimental testing and validation
- Integration with a real system

### References

- Wang, Z., Gao, Q. & Wang, J. A triple-exposure color PIV technique for pressure reconstruction. *Sci. China Technol. Sci.* **60**, 1–15 (2017). <https://doi.org/10.1007/s11431-016-0270-x>
- Charonko, J.J., Antoine, E. & Vlachos, P.P. Multispectral processing for color particle image velocimetry. *Microfluid Nanofluid* **17**, 729–743 (2014). <https://doi.org/10.1007/s10404-014-1355-5>
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